

Wolf-Rayet nebulae as tracers of stellar ionizing fluxes: I. M1-67

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Abstract. We use WR124 (WN8h) and its associated nebula M1-67, to test theoretical non-LTE models for Wolf-Rayet (WR) stars. Lyman continuum ionizing flux distributions derived from a stellar analysis of WR124, are compared with nebular properties via photo-ionization modelling. Our study demonstrates the significant role that line blanketing plays in affecting the Lyman ionizing energy distribution of WR stars, of particular relevance to the study of H II regions containing young stellar populations.

We confirm previous results that non-line blanketed WR energy distributions fail to explain the observed nebular properties of M1-67, such that the predicted ionizing spectrum is too hard. A line blanketed analysis of WR124 is carried out using the method of Hillier & Miller (1998), with stellar properties in accord with previous results, except that the inclusion of clumping in the stellar wind reduces its wind performance factor to only ~ 2 . The ionizing spectrum of the line blanketed model is much softer than for a comparable temperature unblanketed case, such that negligible flux is emitted with energy above the He I $\lambda 504$ edge. Photo-ionization modelling, incorporating the observed radial density distribution for M1-67 reveals excellent agreement with the observed nebular electron temperature, ionization balance and line strengths. An alternative stellar model of WR124 is calculated, following the technique of de Koter et al. (1997), augmented to include line blanketing following Schmutz et al. (1991). Good consistency is reached regarding the stellar properties of WR124, but agreement with the nebular properties of M1-67 is somewhat poorer than for the Hillier & Miller code.

Key words: stars: Wolf-Rayet – stars:fundamental parameters – stars:individual:WR124 – ISM: H II regions – ISM:individual objects:M1-67

1. Introduction

The Lyman ionizing energy distributions of hot, massive stars are important in the study of young starburst regions and galaxies, via population synthesis codes (e.g. Leitherer et al. 1999). However, the interstellar medium (ISM) conspires to prevent this energy from reaching the Earth's atmosphere. Interstellar dust severely degrades transmitted fluxes at ultraviolet and optical wavelengths, while the Lyman continuum of hot stars is completely absorbed by intervening hydrogen atoms for all but a few nearby B stars (e.g. Cassinelli et al. 1995). Therefore, indirect measurements of the extreme UV flux are necessary.

Until recently, the standard method of obtaining the ionizing distributions of hot stars was to rely on line blanketed, plane parallel, LTE model predictions from Kurucz (1991). However, the need to consider non-LTE effects, spherical geometry and line blanketing effects has recently led to the development of complex model atmospheres (e.g. Hubeny & Lanz 1995; de Koter et al. 1997; Pauldrach et al. 1998), with Lyman continuum ionizing flux distributions obtained via synthesis of the accessible UV and optical stellar spectrum. However, these different codes predict quite different ionizing spectra for early-type stars of identical temperatures. While attempts at testing theoretical stellar O-type models via observations of stellar clusters have been made (Stasińska & Schaerer 1998; Oey & Kennicutt 1998), definitive results require studies of *individual* stars and their associated H II regions.

In the case of Wolf-Rayet (WR) stars, evolutionary synthesis models for young starbursts known to contain these stars, known as 'WR galaxies', still rely on unblanketed, non-LTE model atmospheres of Schmutz et al. (1992). What effect does line blanketing have on the predicted Lyman continua of WR stars? Recent theoretical calculations by Crowther (1999) suggest that the effect can

Table 1. Summary of basic stellar and nebular properties of WR124/M1-67.

Quantity	Measurement	Reference
m_v	11.58 mag	Massey (1984)
$(b - v)$	0.81 mag	Massey (1984)
m_K	7.71 mag	van der Hucht et al. (1985)
E_{B-V}	1.18 mag	Crowther et al. (1995b)
Distance	4–5 kpc	Crawford & Barlow (1991)
Sp. Type	WN8h	Smith et al. (1996)
R	55–60 arcsec	Grosdidier et al. (1998)
N_e, T_e	1050 cm ⁻³ , 6200K	Esteban et al. (1991)
$F_{H\alpha}$	2.84×10^{-11} erg cm ⁻² s ⁻¹	Grosdidier et al. (1998)

be substantial, such that unblanketed WR models overestimate the hardness of their ionizing spectra, which is supported by observations of extra-galactic giant H II regions by Bresolin et al. (1999).

In principle, H II regions associated with their central star are ideal tracers of the Lyman ionizing flux distributions. However, suitable nebulae are rare, since their properties are often poorly known. The principal studies for WR stars are those of Rosa & Mathis (1990) and Esteban et al. (1993) who combined WR model fluxes from Schmutz et al. (1989, 1992) with observed properties of WR ring nebulae, to investigate the properties of the central stars. Esteban et al. varied the temperatures of unblanketed WR models until agreement was reached between the observed nebular properties and those predicted by photo-ionization modelling. In general, comparisons with (independent) stellar analyses of the central stars was found to be reasonable, except that lower temperatures were required from the photo-ionization models for late-type WN (WNL) stars, especially the Galactic WN8 star WR124 and its associated H II region, M1-67, for which no agreement was achieved.

In this work, we shall depart from the technique of Esteban et al. in that stellar properties of WR124 are fixed from a spectroscopic study, which are then tested against the nebular properties of M1-67 via photo-ionization modelling using CLOUDY (Ferland 1996). Sirianni et al. (1998) showed M1-67 to be very clumpy. Hubble Space Telescope (HST) imaging of M1-67 by Grosdidier et al. (1998) revealed an astonishingly complex nebula, allowing measurements of the nebular radial density distribution and integrated H α flux. Our work therefore represents the first attempt to test the reliability of predicted WR Lyman continuum distributions using both unblanketed (Hillier 1987) and blanketed models (following Hillier & Miller 1998, 1999) plus robust nebular properties. In our study we compare these predictions with the code of de Koter et al. (1997), augmented to allow for line blanketing following Schmutz (1994, 1997). In this way, we will be able to quantitatively assess the effects of different codes and line

blanketing techniques on the ionizing energy produced by WR stars.

In Sect. 2 we will discuss observations of WR124 and M1-67. In Sect. 3 the model atmospheres codes are introduced and discussed, with stellar results compared in Sect. 4. The photo-ionization modelling technique is discussed and results are presented in Sect. 5. Finally, conclusions are drawn in Sect. 6.

2. Observations of WR124 and its associated nebula, M1-67

We discuss the observed properties of WR124 and M1-67 in this section, and provide a summary in Table 1. Unlike most massive WR nebulae, which are difficult to identify, M1-67 was so striking that it was included in the Bertola (1964) Planetary Nebula catalogue (PK 50+3° 1) with WR124 as its central star. Cohen & Barlow (1975) instead proposed a massive WN origin, which was supported by Solf & Carsenty (1982) and Esteban et al. (1991), who found nebular abundances to be consistent with processed stellar ejecta, indicative of a massive central star. Confirmation of a non-PN origin was made by Crawford & Barlow (1991) who estimated a distance of 4–5 kpc from interstellar Na I D₂ observations. (In order for M1-67 to be a PN, its distance should be ~ 460 pc according to van der Hucht et al. 1985).

2.1. WR124

WR124 (alias 209 BAC, He 2-427) is a Galactic, heavily reddened WN8h star that is well known as the ionizing star of M1-67, with a high heliocentric recession velocity of ~ 200 km s⁻¹ (Merrill 1936). Crowther et al. (1995b) presented optical spectroscopy of WR124, including comparisons with other late-type WN (WNL) stars.

For the current analysis, spectrophotometry obtained in 1991 September at the 2.5m Isaac Newton Telescope (INT), covering $\lambda\lambda 4400-7300$ (resolution 2–3 Å) are used, taken from Crowther et al. (1995b). Observations obtained at the Deutsch-Spanisches Astronomisches Zentrum (DSAZ) 2.2m observatory in June 1991 provide an additional blue dataset covering $\lambda\lambda 3400-4400$ (~ 2 Å resolution), details about which can be obtained from Hamann et al. (1995).

New near-IR spectroscopy of WR124 was obtained in 1998 July at the 3.8m U.K. Infrared Telescope (UKIRT) with the cooled grating spectrograph CGS4, the long (300mm) camera, a 256 \times 256 InSb array and a 401/mm grating. First order observations provided data covering 1.66–2.30 μ m ($R \sim 800$) and 2.98–3.62 μ m ($R \sim 1300$) with a slit width of 0.6'' (1 pixel). This data set was bias-corrected, flat-fielded, extracted and sky-subtracted using CGS4DR (Daly & Beard 1992). Subsequent reductions and analysis were carried out using FIGARO (Meyerdiecks 1993) and DIPSO (Howarth et al. 1995). In order to re-

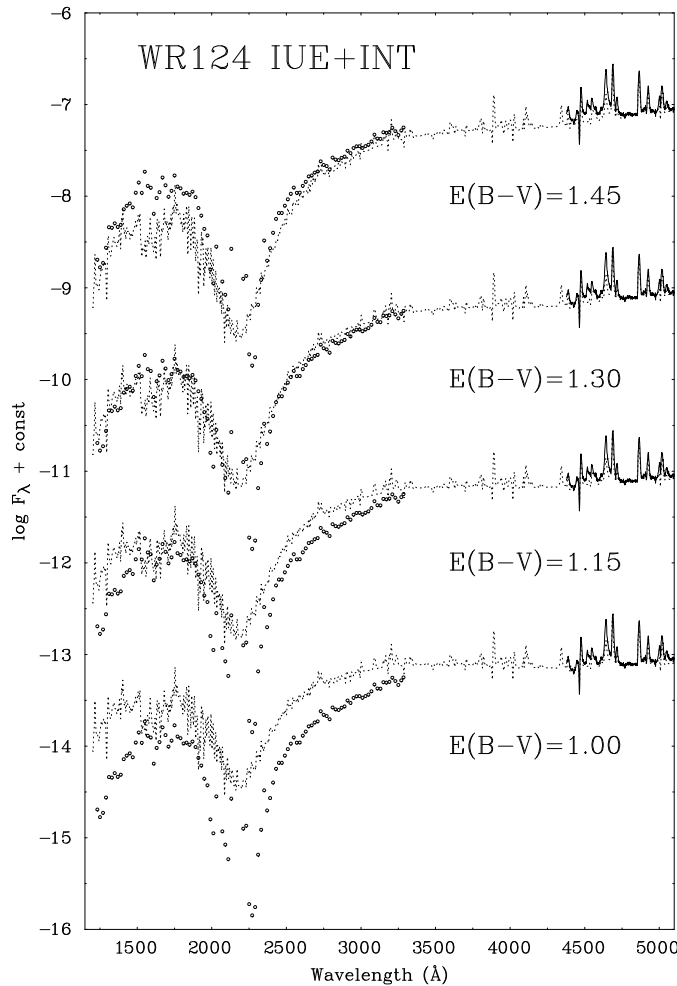


Fig. 1. Comparison between the spectrophotometry of WR124 (open circles: IUE; solid line: INT) and theoretical CMFGEN models, reddened by $E_{B-V}=1.0, 1.15, 1.3$ and 1.45 mag (dotted lines) according to Cardelli et al. (1989). For clarity, comparisons are offset vertically by 0, +2, +4 and +6 units.

move atmospheric features, the observations were divided by a standard star (whose spectral features were artificially removed) observed at around the same time and similar air mass. In regions of low atmospheric transmission at UKIRT the reliability of line shape and strength must be treated with caution (e.g. Paschen α).

The reddening to M1-67 is extremely high, with previous estimates of E_{B-V} in the range 0.90 (Esteban et al. 1991) to 1.50 (Solf & Carsenty 1982). Analysis of the stellar spectrum by Crowther et al. (1995b) indicated $E_{B-V}=1.18$ mag, which implied a distance of ~ 6 kpc, assuming a typical $M_v=-6.0$ mag for WN8 stars. Here we attempt an improved stellar reddening determination by including International Ultraviolet Explorer (IUE) newly extracted spectra (INES, Rodriguez-Pascual et al. 1998) of low resolution (LORES) datasets. The quality of LORES INES datasets are preferred to NEWSIPS (Schartel & Skillen 1998). Four large aperture IUE datasets of WR124

were obtained between 1978–1986, including 3 long wavelength (LWR) datasets, totalling 270 minutes exposure time, plus 1 short wavelength (SWP) dataset of 212 minutes.

Pre-empting the results from the next section, we compare spectrophotometry with reddened, line-blanketed model atmosphere distributions obtained with the CMFGEN code (see Sect. 3.1) in Fig. 1, indicating $E_{B-V}\sim 1.3$ mag ($A_V=4.0$), 0.1–0.2 mag higher than previous results based solely on optical stellar datasets. A comparison with alternative ISA-wind (see Sect. 3.2) model fluxes indicates an equivalent reddening.

Our measurement is in reasonable agreement with the nebular study of M1-67 by Chu & Treffers (1981) who obtained $E_{B-V}=1.23$ from a comparison of its 1.4 GHz and H α flux. In contrast, Esteban et al. (1991) obtained a significantly lower value of $E_{B-V}=0.90$ mag from nebular Balmer line strengths.

Since the reddening towards WR124 is so high, we prefer to select the distance from the K-band absolute magnitude, M_K , where the interstellar reddening is much lower. Using WN8-9 stars at known distance in our Galaxy or the Large Magellanic Cloud (LMC) as calibrators (see Morris et al. 1999 and references therein) we obtain $M_K=-6.2\pm 0.3$ mag. Using the observed K-band magnitude of WR124 from van der Hucht et al. (1985) plus $A_K=0.12\times A_V=0.49$ (Cardelli et al. 1989) we find a distance modulus of 13.44 (i.e. 4.9 kpc), in accord with Crawford & Barlow (1991). Consequently, we adopt a distance of 5 kpc to WR124, i.e. $M_K=-6.25$ mag. Note that the resulting V-band absolute magnitude of $M_V=-6.1$ mag is in excellent agreement with LMC WN8-9 stars (Crowther & Smith 1997).

2.2. M1-67

M1-67, discovered by Minkowski (1946), has a clumpy, ejecta-type, morphology (Chu 1981), with an angular diameter of 90–120 arcsec (Solf & Carsenty 1982; Grosdidier et al. 1998). High spatial resolution spectroscopy of M1-67 was obtained by Esteban et al. (1991), revealing nebular conditions of $N_e\sim 10^3$ and $T_e\sim 6,200$ K. Relative to normal H II regions, oxygen is deficient, with nitrogen enhanced, such that N/O (≈ 3). Their results suggest that O has been processed into N mainly through the ON cycle, and confirm that the M1-67 nebula is composed of stellar ejectra. Esteban et al. estimated an upper limit of 0.2 for the ratio between the ISM mass swept-up by M1-67 and the nebular mass, suggesting that relatively little mixing with the local interstellar gas has occurred.

Fabry-Perot interferometry (Chu & Treffers 1981) and long-slit spectroscopy (Sirianni et al. 1998) indicate a complicated velocity field, with two different motions: a spherical, hollow shell, expanding at 46 km s $^{-1}$, plus a ‘bipolar’ outflow with a larger velocity of 88 km s $^{-1}$. Sirianni et al. (1998) interpreted this structure as the result of two

subsequent outbursts. Grosdidier et al. (1998) used the very high spatial quality of the Wide Field and Planetary Camera 2 (WFPC2) aboard HST to reveal filamentary, chaotic substructures, with a number of ‘bullets’ in the nebula, which seem to concentrate within two conical regions in agreement with the previous results of Sirianni et al. (1998). Globally, Grosdidier et al. (1998) found that the de-projected radial density distribution of M1-67 is well described by a power law, $N_e(r) \sim r^{-0.8}$, with a cutoff at $r \geq 50''$.

3. Stellar atmosphere codes

In this section we introduce and utilise the codes that are used to carry out spectral synthesis of WR124. CMFGEN (Hillier 1987, 1990; Hillier & Miller 1998, 1999) solves the transfer equation in the co-moving frame, subject to statistical and radiative equilibrium, assuming an expanding, spherically-symmetric, homogeneous or clumped, atmosphere. Populations and ionization structure are consistent with the radiation field.

To take into account the (microscopic and macroscopic) velocity structure expected in a real WR star, a uniform Doppler line width of $V_{\text{Dop}} = 50 \text{ km s}^{-1}$ is assumed. Since this is substantially greater than the (species dependent) thermal Doppler width, we refer to it as a ‘broad-line’ approximation. All lines within some multiple of V_{Dop} can interact within the Sobolev resonance zone. Because of the large line width used, the interaction between two lines may be overestimated in the broad-line approximation.

A simplifying ‘super level’ approach is used for individual levels (Anderson 1989), particularly for iron-group elements. In this approach, several levels of similar energies and properties are treated as a single ‘super level’, with only the populations of the super level included in the solution of the rate equations. The population of an individual atomic level in the full model atom is determined by assuming that it has the same departure coefficient as the corresponding super level to which it belongs.

Unfortunately, individual line blanketed co-moving frame calculations are generally computationally demanding, despite the use of super levels, so we first need to confirm that individual case studies, such as this, are in accord with observation. A computationally quick method is to (i) solve the transfer problem in the Sobolev approximation rather than the co-moving frame, which the code ISA-wind does (de Koter et al. 1993, 1997), and (ii) consider line blanketing via Monte Carlo sampling following Schmutz (1994, 1997) allowing the opacity of a huge number of lines to be considered. How consistent are results obtained with these different methods?

3.1. CMFGEN

The model calculations are based on the iterative technique of Hillier (1987, 1990) named CMFGEN. Allowance is made for line blanketing and clumping following the formulation of Hillier & Miller (1998) to which the reader is referred for specific details. The model atom contains hydrogen, helium, carbon, nitrogen, silicon and iron as shown in Table 2. Details of each ion are included, such that for hydrogen, $n=1$ to 30 full levels are considered, which are grouped into 10 super levels. Test calculations indicated that ~ 5000 iron transitions with $gf \leq 10^{-4}$ have negligible influence on the emergent spectrum, but required considerable computational effort, so these have been excluded. Within a super-level, representing a group of full levels, populations are assumed to be in LTE. Elemental abundances other than hydrogen and helium are fixed at cosmic (Si=0.1% by mass, Fe=0.2% by mass) or approximately CNO-equilibrium (C=0.03%, N=1 to 2% by mass) values for a solar metallicity environment.

The stellar radius (R_*) is defined as the inner boundary of the model atmosphere and is located at Rosseland optical depth of ~ 20 with the stellar temperature (T_*) defined by the usual Stefan-Boltzmann relation. Similarly, the effective temperature (T_{eff}) relates to the radius ($R_{2/3}$) at which the Rosseland optical depth equals $2/3$.

3.2. ISA-wind

The improved Sobolev approximation code (ISA-wind) is described in detail by de Koter et al. (1993, 1997). The principal differences with CMFGEN relate to: (a) the treatment of the line radiation transfer; (b) the wind electron temperature, which assumes a grey, LTE atmosphere rather than radiative equilibrium, where the temperature is fixed at a pre-assigned value in the outer regions, such that lines originating in the outer wind (e.g. He I $\lambda 10830$) may be incorrectly predicted; (c) the velocity structure deep in the atmosphere; (d) the specific atomic model treated, as listed in Table 2; (e) the neglect of clumping.

ISA-wind solves the line radiation transfer using an improved version of the Sobolev approximation. In co-moving frame codes, line photons with a finite (given) width interact with the continuum over a range of depth and frequency points, while in the Sobolev approximation the continuum opacity and source function are considered constant within the line resonance volume. In the improved version of the Sobolev code, ISA-wind, absorption of line radiation by the continuum is taken into account within the resonance volume. The Sobolev approximation should be ideal for the large velocity gradients of WR outflows. It introduces great simplification in the rate equations, and makes the overall iteration process about 10 times faster than a co-moving frame code, for the same number or ionic levels and grid points.

Table 2. Summary of model atom used in CMFGEN and ISA-wind radiative transfer calculations, including full levels (N_F), super levels (N_S) and total number of transitions (N_{Trans}), following Hillier & Miller (1998) and de Koter et al. (1997). Note that transitions considered in CMFGEN include those between individual terms in multiplets. The Monte Carlo calculation used to derive line blanketing accounts for transitions of most metals, including Al, Si and Fe.

Ion	N_S	N_F		N_{Trans}		Details	
	CMFGEN	CMFGEN	ISA-wind	CMFGEN	ISA-wind	CMFGEN	ISA-wind
H I	10	30	10	435	45	$n \leq 30$.	$n \leq 10$
H II	1	1	1				
He I	29	51	51	579	691	$n \leq 20$.	$n \leq 20$
He II	13	30	20	435	190	$n \leq 30$.	$n \leq 20$
He III	1	1	1				
C III	21	38	–	147	–	$nl \leq 2s4f^1 F^\circ$	–
C IV	9	14	12	48	66	$n \leq 4$.	$n \leq 7$
C V	1	1	1				
N II	23	41	3	144	3	$nl \leq 2p3d^1 P^\circ$	$nl \leq 2p^2 \ ^1S$
N III	33	48	40	407	561	$nl \leq 2p4p^2 D$	$nl \leq 2p4p^2 P$
N IV	22	38	34	144	561	$nl \leq 2p3d^1 D^\circ$	$nl \leq 2s4f^1 F^\circ$
N V	9	15	26	42	325	$n \leq 5$	$n \leq 10$
N VI	1	1	1				
Al III	17	45	–	362	–	$n \leq 10$	–
Al IV	1	1	–				
Si III	25	45	–	170	–	$nl \leq 3s5f^1 F^\circ$	–
Si IV	17	28	–	129	–	$n \leq 6$	–
Si V	1	1	–				
Fe III	52	242	–	1840	–	$nl \leq 3d^5(^4F)5s^5F$	–
Fe IV	21	280	–	3538	–	$nl \leq 3d^4(^1G)4p^2P^\circ$	–
Fe V	19	182	–	1803	–	$nl \leq 3d^3(^2D)4p^1P^\circ$	–
Fe VI	10	80	–	722	–	$nl \leq 3d^2(^1S)4p^2P^\circ$	–
Fe VII	1	1	–				
	337	1214	181	10945	2442		

Turning to line blanketing, an iterative technique including the Monte Carlo method of Schmutz et al. (1991) and Schmutz (1994, 1997) is used. The method allows the computation of intensity-weighted effective opacity factors, which account for the presence of tens of thousands of spectral lines, dominated by Fe and Ni. Based on ISA-wind atmosphere calculations, the Monte Carlo (MC) code determines the line blanketing factors. An iterative procedure is used, such that blanketing factors are used by the non-LTE code to calculate a new atmosphere, which in turn is used to calculate new blanketing factors. A few iterations are generally sufficient. This is due to the fact that the scattering and absorption factors are not very sensitive to the specific model parameters.

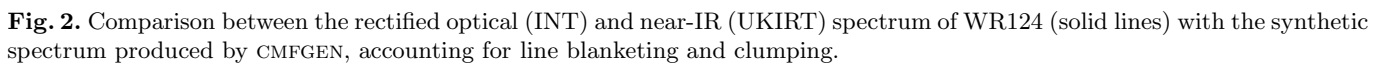
The MC method deals with the radiative transfer in the correct manner, except that the ionization and excitation equilibrium of metal species is approximate. This dictates which lines are efficient at capturing photons for each point in the atmosphere. The ionization structure of H and He in the MC code is derived from ISA-wind. For other species, an representative ionization temperature is used, obtained from the principal ionization stages for each metal that is considered in ISA-wind. The MC

code calculated ionization stratification can therefore be compared with that of ISA-wind for consistency.

Since line-line interactions are not accounted for in the MC calculation, explicit correction factors, named ‘photon loss’ factors, need to be considered to allow for interaction between important resonance lines (He II $\lambda 303$, He I $\lambda 584$) and nearby metal lines (Schmutz 1997). We have calculated photon loss factors from the opacities of He II $\lambda 303$ and lines at nearby wavelengths, and find that line-line interactions are negligible for the stellar temperatures of WNL stars. (Pasquali et al. (1997) previously adopted a factor of 10^{-4} at He II $\lambda 303$ for WNL stars.) Additionally, we have determined that line-line interaction between He I $\lambda 584$ and adjacent metal lines would not affect the ionization balance or derived stellar parameters for WR124.

4. Stellar analysis

Unblanketed non-LTE spectroscopic analyses of WR124 by Hamann et al. (1993) and Crowther et al. (1995a) revealed $T_* \approx 30\text{--}34\text{ kK}$, $\log(L/L_\odot) \sim 5.3\text{--}5.4$, $\dot{M} \sim 10^{-4.2} M_\odot \text{ yr}^{-1}$, and $v_\infty \sim 700 \text{ km s}^{-1}$. The latter study included hydrogen, helium, carbon and nitrogen, deriving H/He ~ 0.6 by number. Hamann & Koesterke (1998a) as-



4.1. Analysis technique

Our approach follows that of Crowther et al. (1995a), such that diagnostic optical lines of He I ($\lambda 5876$), He II ($\lambda 4686$) and H I ($H\beta + \text{He II } \lambda 4859$) are chosen to derive the stellar temperature, mass-loss rate, luminosity and hydrogen content. In the absence of high resolution UV observations, a wind velocity of 710 km s^{-1} is obtained from optical He I P Cygni line profiles. A $\beta=1$ velocity law is adopted, since this reproduces the optical, near-IR and mid-IR spectra of a similar WN8 star, WR147 (Morris et al. 1999).

Table 3. A comparison of stellar parameters obtained for WR124 using CMFGEN (unblanketed and blanketed) and ISA-wind (blanketed). The unblanketed results are taken from Crowther et al. (1995b), based on identical observations. In all cases, a standard velocity law with $\beta=1$ is assumed.

Parameters	CMFGEN		ISA-wind
Filling factor, f	100%	10%	100%
Blanketed?	no	yes	yes
T_* (kK)	33.5	32.7	32.8
R_* (R_\odot)	17.1	18.0	16.2
$\log(L_*/L_\odot)$	5.52	5.53	5.44
$\log(\dot{M}/\sqrt{f}) M_\odot \text{yr}^{-1}$	-4.1	-4.2	-4.4
v_∞ (km s $^{-1}$)	710	710	710
H/He	0.6	0.7	0.8
N/He	0.004	0.006	0.003
$\log Q_0$ (s $^{-1}$)	49.05	49.05	49.00
$\log Q_1$ (s $^{-1}$)	48.19	43.88	47.91

approximation for WR analyses, and represents an important result from the present study.

In Fig. 3, we compare identical optical observations of WR124 with the synthetic spectrum obtained from the ISA-wind contour plot, allowing for line blanketing. The quality of line fits is comparable to CMFGEN, except that (i) the region around $\lambda 4100$ is more severely underestimated, due to the neglect of Si IV $\lambda 4088\text{--}4116$, (ii) He I $\lambda 5015$ is too weak; (iii) He II $\lambda 4200$, $\lambda 4542$ and $\lambda 5412$ are in better agreement than CMFGEN. In the near-IR, He I $2.058\mu\text{m}$ emission is predicted to be somewhat too strong, as is He I $2.112\mu\text{m}$ emission, with Br γ too weak.

4.3. Comparison of ionizing flux distributions

Our three solutions indicate very similar stellar properties for WR124 and are equally successful at reproducing its optical spectrum. How do the Lyman ionizing flux distributions of these models compare?

The unblanketed CMFGEN ionizing energy distribution is shown in Fig. 5. It is relatively flat, with a small jump beyond the He I edge at 1.81 Ryd (24.6 eV or 504 Å), and a non-negligible flux up to 3.2 Ryd (286 Å). Fig. 5 reveals that the blanketed CMFGEN distribution is much softer than the unblanketed solution, showing a large deficit for energies $\geq 1.3\text{Ryd}$ (i.e. $\lambda \leq 700\text{Å}$), such that a very low flux is emitted at energies beyond the He I edge. In addition, this distribution shows a moderate excess between the Lyman edge and 1.25 Ryd relative to the unblanketed case, which explains why its bolometric luminosity is essentially identical.

ISA-wind shows an intermediate energy distribution, with a depression around 1.7 Ryd (540 Å), but a relatively hard flux beyond the He I edge, up to energies of 2.9 Ryd (310 Å). Possible explanations for the differences in ionizing fluxes between the two blanketed cases are discussed in Sect. 5.4.

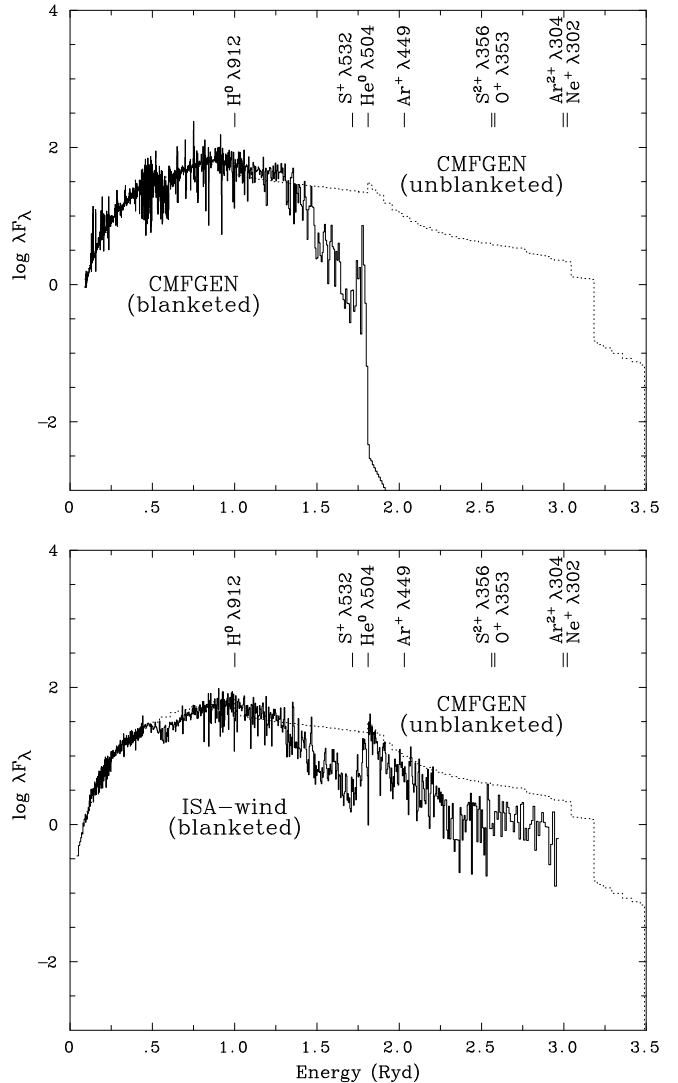


Fig. 5. (upper panel:) Comparison between the Lyman ionizing distribution of unblanketed CMFGEN (dotted lines) and blanketed CMFGEN (solid lines) for WR124, revealing large differences; (Lower panel) as above, except for unblanketed CMFGEN (dotted lines) and blanketed ISA-wind (solid lines). Note that these diagrams are designed to emphasise the extreme UV spectral region, important for the nebular ionization, and not the overall energy distribution.

5. Photo-ionization modelling

From the usual diagnostic diagram relating $\text{H}\alpha/[\text{S II}]$ to $[\text{S II}] \lambda 6717/\lambda 6731$ (see Sabadhin et al. 1977) we find that M1-67 falls in the photo-ionization dominated region. Therefore we use the general purpose photo-ionization code CLOUDY (Ferland 1996) for our analysis. The ionising radiation fields presented in the previous section are expected to yield different predicted nebular properties, when input into CLOUDY, which can be quantitatively compared with spectroscopic nebular observations taken from Esteban et al. (1991).

5.1. Description of the calculations

We constructed photo-ionization models using CLOUDY (v90.04) as described in Ferland (1996) and Ferland et al. (1998). Comparisons with other photo-ionization codes are provided by Ferland et al. (1995). The nebula are represented by a sphere of variable gas density, n , and filling factor, ϵ , with a central cavity that is ionized and heated solely by the UV radiation of a single central star. Nebular fluxes are predicted, given input abundances, flux distributions and physical parameters. We use a volume filling factor of $\epsilon=0.05$ as estimated by Solf & Carsenty (1982). The de-projected radial density profile obtained by Grosdidier et al. (1998) was used, together with an outer (inner) nebula boundary at $50''$ ($8''$), which corresponds to 1.25 pc (0.2 pc) using a distance of 5 kpc.

Grosdidier et al. (1998) provided a measurement of the integrated nebular H α flux, after correction for [N II] contamination. We obtain an integrated de-reddened H α flux using the reddening of $E_{B-V}=1.3$ mag, determined in Sect. 2.1, namely $I(\text{H}\alpha)=5.45\times10^{-10}$ erg cm $^{-2}$ s $^{-1}$. In addition, long slit nebular line intensities of Esteban et al. (1991) (their position A) are de-reddened according to this value of E_{B-V} . Although the majority of previous stellar and nebular reddening determinations are in reasonable agreement with our value, Esteban et al. (1991) obtained a substantially lower value of $E_{B-V}=0.90$ mag for M1-67 using H α /H β . Consequently, the H α /H β ratio, de-reddened according to our stellar reddening of $E_{B-V}=1.3$ is far from the usual Case B value.

In order to assess the impact of alternative reddening determinations on the nebular properties, we have also calculated the integrated H α flux, following the reddening determination of Esteban et al. (1991), i.e. $E_{B-V}=0.9$, so that $I(\text{H}\alpha)=2.35\times10^{-10}$ erg cm $^{-2}$ s $^{-1}$. For this case, long slit nebular line intensities are taken directly from Esteban et al. (1991). Note that identical stellar ionizing flux distributions to those obtained for the higher reddening case are used in this analysis, except that the absolute K-band magnitude is adjusted by 0.15 mag to $M_K = -6.1$ mag, for consistency with the adopted distance of 5 kpc. Results from this alternative approach are very similar to those discussed here for $E_{B-V}=1.3$ mag.

The electron density at the inner boundary was selected so that the predicted H α flux agreed with observations. For the $E_{B-V}=0.9$ mag case, typical quantities are $N_e=1,350$ cm $^{-3}$ at the inner boundary ($8''$ or 0.2 pc), and 320 cm $^{-3}$ at the outer boundary ($50''$ or 1.25 pc). Similar values were measured by Esteban et al. (1991), namely $\sim 1,000$ cm $^{-3}$ at a distance of 10–25'' and ~ 200 cm $^{-3}$ for $\geq 30''$ (their region W).

Abundances are assumed to be typical of Galactic H II regions, except for N, O and S, which are adapted from Esteban et al. (1991). For each reddening, electron densities and temperatures were obtained from the de-reddened [S II] $\lambda 6716/\lambda 6731$ and [N II] $\lambda 5755/\lambda 6584$ ratios using the

Table 4. Comparison between observed and predicted nebular properties of M1-67 from CLOUDY, based on various ionizing flux distributions. Nebular line measurements are taken from slit position A of Esteban et al. (1991), de-reddened according to $E_{B-V}=1.3$ (Sect. 2.1) and given relative to H $\beta=100$, including *formal* errors from Esteban et al., neglecting systematic (calibration) uncertainties. I(H β) represents the de-reddened, integrated H β flux received at the Earth (erg cm $^{-2}$ s $^{-1}$), obtained via the H α flux measured by Grosdidier et al. (1998).

Quantities	Observed	CMFGEN	CMFGEN	ISA-wind
Blank?		no	yes	yes
log I(H β)	−9.7	−9.7	−9.7	−9.7
ϵ		0.05	0.05	0.05
$N_e(r=0.2\text{pc})$		2050	1650	2000
$N_e(r=1.25\text{pc})$		480	380	460
12+log N/H	8.21	8.21	8.21	8.21
12+log O/H	8.09	8.09	8.09	8.09
12+log S/H	6.64	6.64	6.64	6.64
He/H	0.2	0.2	0.2	0.2
3727 [O II]	21±2	37	52	52
5007 [O III]	≤1:	316	0.0	148
5755 [N II]	0.7±0.1	1.1	1.9	1.3
5876 He I	1.6±0.3	30	0.0	31
6548 [N II]	71±1	24	113	45
6563 H α	194±1*	284	292	287
6584 [N II]	204±2	71	333	134
6717 [S II]	8.4±0.2	1.8	12.5	2.7
6731 [S II]	10.3±0.2	1.9	12.8	2.8
7135 [Ar III]	0.2:	68	0.1	50
9069 [S III]	5.5±0.3	30	9.5	24
9546 P8	1.9±0.2	3.8	3.9	3.9
N $^{2+}$ /N $^{+}$		10	0.00	3
O $^{2+}$ /O $^{+}$	≤0.02	5.5	0.00	1.5
S $^{2+}$ /S $^{+}$	0.9	35	1.2	17
Ar $^{2+}$ /Ar $^{+}$		57	0.00	25
T_e (K)	6,200	9,800	6,900	8,500

*: See text for an explanation why the H α flux does not agree with the Case B value using our stellar reddening.

RATIO program (Adams & Howarth, priv. comm.). For $E_{B-V}=0.9$ we obtained $N_e=10^{2.9}$ cm $^{-3}$ and $T_e=6,000$ K, while $N_e=10^{3.0}$ cm $^{-3}$ and $T_e=6,200$ K for $E_{B-V}=1.3$. Subsequently, ionic abundances were obtained by solving the equations of statistical equilibrium using the EQUIB program (Adams & Howarth, priv. comm.), and are given in Table 4 for each reddening. The usual elemental diagnostics were chosen, [N II] $\lambda 6584$, [O II] $\lambda 3727$, [S II] $\lambda 6731$ and [S III] $\lambda 9069$, with no ionization correction factors for nitrogen (since O $^{2+} \ll$ O $^{+}$). Also, we have adopted He/H ~ 0.2 , since helium is expected to be moderately enriched. Solar abundance ISM dust grains were assumed, although the precise choice is not critical.

5.2. Results from photo-ionization modelling

Esteban et al. (1993) identified a large discrepancy between the nebular fluxes of M1–67 as determined by unblanketed model atmospheres (Schmutz et al. 1992) and that observed. In particular, they were unable to reproduce the observed T_e and S^+/S^{2+} ratio. Closest agreement was achieved for the line blanketed model of R84 (WN9) from Schmutz et al. (1991). We now investigate whether this discrepancy remains, based on improved stellar models, including those for which line blanketing is incorporated. Comparisons between predicted and observed nebular properties are presented in Table 4, including results from both the reddening of Esteban et al. (1991), or the present value, to illustrate the possible range of line strengths and plasma conditions. Lamers et al. (1999) discuss various aspects of the reliability of generally derived nebular conditions and abundances, of relevance to the present comparisons.

5.2.1. CMFGEN

From Table 4, the discrepancy between the observed plasma conditions and photo-ionization modelling from the unblanketed CMFGEN analysis is more acute than Esteban et al. (1993) obtained, for both reddening solutions. (A higher stellar temperature is imposed here by modelling the stellar spectrum, including the allowance for light metals, whereas Esteban et al. did not adopt any stellar constraint).

In this case, the ionization balance in the nebula is much higher than observed, with S^{2+}/S^+ overestimated by a factor of 40. In addition, the mean T_e is far too high, with the predicted range from 11,200K at the inner nebula to 9,500K at the outer boundary, contrasting sharply with the observed value of 6,200K. Recalling Fig. 5, a relatively strong flux at energies greater than the S^{2+} edge at 356Å indicates that the predicted nebular ionization balance implies $S^{2+} \gg S^{3+} > S^+$. Similarly for oxygen, the strong flux predicted below the O^+ edge at 353Å implies an error in the O^{2+}/O^+ ratio of order ≥ 300 ! Consequently, [O III] $\lambda 5007$ is predicted to have an intensity that is greater than $H\beta$, yet [O III] $\lambda 5007$ is barely detected in M1–67. Similar problems relate to [N II] $\lambda 6584$, He I $\lambda 5876$ and [Ar III] $\lambda 7135$.

In contrast, the line blanketed CMFGEN model, with a much softer extreme UV energy distribution, produces a much lower predicted electron temperature, in the range 6,600–7,900K, now in reasonable agreement with observations. From Table 4, almost every nebular line is predicted to be within a factor of two of the de-reddened value, with the predicted ionization balance in good agreement with observations.

An explanation for the success of this model can be understood by recalling Fig. 5 in which negligible flux is predicted at energies greater than the He^0 edge at 504Å,

and indeed only a small flux beyond the S^+ $\lambda 532$ edge. Consequently, [S II] $\lambda 6731$ and especially [S III] $\lambda 9069$ are fairly well matched for either case, although the predicted ionization balance is actually marginally too low: $S^+ \simeq S^{2+} \gg S^{3+}$. Another important success of this model is that negligible flux is predicted above the O^+ 353Å edge, so that the observed absence of [O III] $\lambda 5007$ is accounted for.

However, the ionization of the model predicts negligible He I $\lambda 5876$ and [Ar III] $\lambda 7135$ emission, yet these are both observed, albeit weakly. Note that the precise choice of the He/H abundance ratio in the nebula does not play a major role in the predicted He I $\lambda 5876$ strength, since it is primarily determined by the number of He I ionizing photons. Less crucial deficiencies of this model are that [N II] $\lambda 6584$ and [O II] $\lambda 3727$ are predicted to be too strong, although [N II]/ $H\alpha$ (independent of reddening uncertainties) is in good agreement.

5.2.2. ISA-wind

Turning to ISA-wind, its energy distribution lies intermediate between the unblanketed and blanketed CMFGEN models, such that the nebular ionization structure is predicted to be somewhat higher than the observed properties, with T_e overestimated by 40%. Once again, a significant ionizing flux is predicted to lie at energies above the O^+ edge, so that the predicted O^{2+}/O^+ ratio is a factor of ≥ 75 times too high, with very strong [O III] $\lambda 5007$ predicted. Similarly, the flux above the S^{2+} and He^0 edges are too strong, so that the S^{2+}/S^+ ratio is in error by a factor of 20, and He I $\lambda 5876$ is strongly overestimated.

5.3. Influence of uncertain nebular properties

How dependent are the predicted nebular properties on our assumed filling factor, ϵ , or geometry? As a test, we have carried out calculations for the blanketed CMFGEN case with $E_{B-V}=1.3$ mag.

For $\epsilon=0.025$ (a factor of two smaller), the required electron density is $\sqrt{2}$ higher, while predicted nebular properties and line strengths properties are barely affected, with the electron temperature unchanged. The greatest influence of a decrease in filling factor is a decrease in the sulphur ionization balance, from $S^{2+}/S^+=1.2$ to 0.9, with changes in nebular line strengths of up to 20% for [S II–III]. Comparable increases in S^{2+}/S^+ and decreases in electron density are obtained for higher filling factors.

Similarly, we have compared results with a constant, rather than exponentially decreasing, density throughout the nebula. For $\epsilon=0.05$, the required electron density is $N_e=530 \text{ cm}^{-3}$. Again, the influence is generally small, with the electron temperature unchanged and line strengths modified by up to 10%. Once again, the effect on sulphur is greatest, such that the ionization balance is

decreased from $S^{2+}/S^+=1.2$ to 1.0 and changes in $[S\text{ II-III}]$ strengths of up to 20%.

From these calculations, we consider that the nebular predictions are robust, for the blanketed CMFGEN case at least, except that the sulphur line strengths and ionization balance suffer from uncertainties of order $\pm 50\%$. Equivalent tests for the unblanketed CMFGEN case indicate similar uncertainties for the ionization balance of oxygen and nitrogen, although the effect on emission lines from $[O\text{ II-III}]$ is minor.

Finally, one further note of caution is necessary. Lamers et al. (1999) emphasise that nebular line fluxes and (absolute) abundances may be sensitive to clumping, of particular concern for the M1-67 nebula. Although beyond the scope of the present work, one would ideally like to carry out a re-evaluation of the nebular abundances and conditions of M1-67, accounting for its highly clumped nature.

5.4. Why are predicted ionizing fluxes different?

A definitive explanation for the difference in ionizing spectra produced by the blanketed CMFGEN and ISA-wind models shortward of $\lambda 700\text{\AA}$ is not straightforward, given the differences in their treatment of the radiative transfer, blanketing, atomic models and atomic data. Nevertheless, several differences in the alternative techniques deserve consideration.

The most promising reason for the differences is that CMFGEN allows for photons that are absorbed in lines and re-emitted at other (longer) wavelengths. In contrast, no such channel is available in the ISA-wind MC calculations, thereby overestimating the ionizing flux. Other possible explanations, such as photon loss operating in CMFGEN at the He I $\lambda 584$ resonance line, or an incorrect iron ionization balance being used for the MC calculation in ISA-wind, appear to be excluded (Sect. 3.2).

In addition, the number of lines treated in both cases is incomplete, so that blocking will be underestimated, and the predicted ionizing fluxes overestimated. Recall that the number of lines considered by CMFGEN is relatively small, principally treating Fe III-V, while ISA-wind considers many more lines and ionization stages, although this is clearly not complete (solely lines between measured energy levels are included). Depending on the strength of this effect, softer ionizing energy distributions would result, leading to improved agreement with nebular properties for ISA-wind.

In spite of the modelling and nebular difficulties, we conclude that the CMFGEN line blanketed ionizing energy distribution for WR124 provides excellent consistency with the nebular properties of M1-67, and solves the problem that was identified by Esteban et al. (1993) for this system based on unblanketed models. Use of ISA-wind leads to consistent stellar properties for WR124, al-

though the consistency with observed plasma conditions for M1-67 are somewhat poorer than for CMFGEN.

6. Conclusions

We have used WR124 and its associated nebula M1-67 to assess the reliability of Lyman ionizing flux distributions from current stellar models. For WR124, we find that stellar properties obtained with two line blanketed, non-LTE extended model atmospheres, ISA-wind (de Koter et al. 1997) and CMFGEN (Hillier & Miller 1998) are in excellent agreement. However, comparisons with the observed properties of M1-67 favour the ionizing energy distribution obtained by CMFGEN rather than ISA-wind, reconciling previous inconsistencies identified by Esteban et al. (1993). Certainly, more general conclusions await comparisons for a variety of stars.

In the future we propose to extend our study to WR stars of different spectral type. One well known example is HD 192163 (WR136) and its ring nebula NGC 6888, for which Esteban et al. (1993) also identified a major inconsistency. However, in contrast with M1-67, there is evidence that nebular emission in NGC 6888 may be produced by shocks rather than photo-ionization. Further, the properties of other Galactic WR nebulae are often poorly known, such that different stellar ionizing distributions can reproduce the nebular properties by selecting, for example, alternative electron densities or shell thickness. WR nebulae in the LMC may provide more suitable candidates (Dopita et al. 1994).

In general, study of young stellar populations in external galaxies via associated H II regions relies heavily on suitable stellar ionizing flux distributions (e.g. Leitherer et al. 1999). Currently, the only WR models that are generally available at this time are unblanketed, pure helium energy distributions (Schmutz et al. 1992). The calculation of a large multi-parameter grid of line-blanketed models remains a formidable computational challenge, unless codes such as ISA-wind can be relied upon. Crowther (1999) finds that, in general, the H I and He I ionizing fluxes of early-type WR stars are not greatly affected by line blanketing. However, the additional blanketing from C and O in early WC stars produces a softer ionizing spectrum than for early WN stars of identical temperatures, with negligible flux emitted $\lambda \leq 300\text{\AA}$. Indeed, unblanketed models are probably to be preferred for the study of young starburst regions in very metal deficient regions. However, the (uncertain) role that metallicity may play on mass-loss rates of Wolf-Rayet stars does need to be quantitatively investigated (e.g. Crowther et al. 1999).

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